

Research Article

# The Effect of Numerical Mapping Techniques on Performance in Genomic Research

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# Abstract

In genomic signal processing applications, digitization of these signals is needed to process and analyze DNA signals. In the digitization process, the mapping technique to be chosen greatly affects the performance of the system for the genomic domain to be studied. The purpose of this review is to analyze how numerical mapping techniques used in digitizing DNA sequences affect performance in genomic studies. For this purpose, all digital coding techniques presented in the literature in the studies conducted in the last 10 years have been examined, and the numerical representations of these techniques are given in a sample DNA sequence. In addition, the frequency of use of these coding techniques in four popular genomic areas such as exon region identification, exon-intron classification, phylogenetic analysis, gene detection, and the min-max range of the performances obtained by using these techniques in that area are also given. This study is thought to be a guide for researchers who want to work in the field of bioinformatics.

**Keywords**: Numerical mapping techniques, Genomic analysis, DNA encoding schemes, Genomic signal processing, DNA sequence

### 1. Introduction

Deoxyribose nucleic acid (DNA) is the biological structure that is located inside the cells, which are the building blocks of the human body, and creates the genetic code in which all human characteristics are encoded. DNAs consist of sugar groups, phosphate groups and bases linked by ester bonds. These bases are Adenine, Thymine, Guanine, and Cytosine. In the DNA chain consisting of two long polymers, Adenine pairs with Thymine while Guanine pairs with Cytosine. The codes created by certain combinations of the building blocks called nucleic acids that makeup DNA are called genes. Genes; These are personal codes that determine all the characteristics of the body, such as eye color, height, hairstyle, or susceptibility to genetic diseases. A gene has exons and introns. The intron is the non-amino acid coding portion of a gene. Exons are the protein-coding parts of the gene. The triple arrangement of bases in DNA is referred to as codons and these codons code for the different amino acids that make up proteins. There are 64 possible codons in a DNA. Three of the codons (UAA, UAG, UGA) are termination or stop codons and do not code for any amino acid. Each of the remaining 61 codons codes for an amino acid, but since there are only 20 amino acids used in protein construction, there is more than one codon encoding the same amino acid [1]. Genetic information from DNA is transferred to RNA. This process is called transcription. The translation is the process of translating the code carried by the mRNA into proteins. Figure 1 shows the basic structure of a protein-coding gene related to transcription and translation in a eukaryotic organism.



Figure 1 Gene and intergenic regions in a DNA

# **1.1. Literature Review**

In this section, studies that examine the techniques used for digitization of DNA data in various genomic fields such as detection of exon regions from DNA sequences, exon-intron classification, phylogenetic analysis, interspecies similarity/difference, detection of disease, and gene detection are presented. Table 1 lists all studies over the past 15 years examining numerical mapping techniques used by genomic domains.

| Reference<br>Paper    | Numerical mapping techniques  | Genomic domain                      |
|-----------------------|---|-------------------------------------|
|                       | 1. The Nucleotide Mapping   |                                     |
| Das et al.[3]         | Diploye moment mapping, Minimum entropy mapping, Trigonometric<br>mapping, Variable mapping, Chaos game representation, Gray code<br>mapping, Walsh code mapping, Pseudo-EIIP mapping<br>2. The Amino acid Mapping  | Prediction of Exon regions          |
|                       | Dipola moment and alpha mapping, Binary representation, Genetic code<br>context, EIIP, Complex prime numeric representation, Hyropathy index,<br>P-adic mapping, Ionization-constant, The tetrahedron mapping   |                                     |
| Wisesty et al.<br>[4] | Voss mapping, Z-curve, tetrahedron, Complex number representation,<br>Integer and real representation, Trigonometric mapping, Paired numeric<br>representation  | Diagnosis of breast cancer          |
| Kumar et al.<br>[5]   | Position Based Encoding, 2-bit Neural Network based encoding,<br>Hamming Distance Based Encoding, Integer Number Encoding,<br>Trigonometric Encoding, Autocorrelation Based Encoding and proposed<br>Method walsh code  | Detection of protein coding regions |
| Yu et al. [6]         | <ol> <li>Biochemical Properties</li> <li>Atomic number, Electron-Ion Interaction pseudopotential, Molecular<br/>mass representation, Thermodynamic properties</li> <li>Primary-Structure Properties</li> <li>Dinucleotide representation, Ring structure, Inter nucleotide distance<br/>encoding, Triplet encoding, Frequency of occurence mapping, Minimum<br/>entropy mapping</li> <li>Cartesian-Coordinate Properties</li> <li>Integer and real number, Complex number, QPSK/PAM, DNA walk and<br/>paired numeric Method</li> <li>Binary and Information Encoding</li> <li>Voss representation, Galois field, Error-Correction code, Ching<br/>representation</li> </ol> | Genomic signal processing           |

Table 1 All studies reviewed in the last 15 years

| Kumari et al.<br>[7]                           | <ol> <li>Graphical Representation</li> <li>CGR and CGR-walk, Tetrahedron, SOM based approach, Quaternion, H-<br/>curve and Z-curve</li> <li>1.Fixed Mapping</li> <li>Voss, Tetrahedron, Complex, Integer, Real, Quaternion, QPSK</li> <li>2.Cariable Mapping</li> <li>Complex representation of nucleotides by twiddle factor</li> <li>3.Physico Chemical Property Based Mapping</li> <li>Atomic, Paired, DNA walk, Z-curve, EIIP, Pseudo-EIIP</li> </ol> | Genomic signal processing                      |
|--|---|--|
| Das et al. [8]                                 | Voss, Integer, Complex, Real, EIIP, Atomic Number, Paired Numeric,<br>DNA Walk, Molecular Mass, Trigonometric, Entropy, Z- curve,<br>Tetrahedron  | Predicting of protein coding regions           |
| Ahmad et al.<br>[9]                            | Tetrahedron, 4-bit binary coding, Binary coding, Molecular mass, Z-<br>curve, Pathogenity island coding, Entropic segmenttion coding, Paired<br>nucleotide representation, Integer number, Autoregressive coding,<br>Gradient source Localization, EIIP, Paired nucleotide atomic number,<br>Complex number   | Genomic signal processing                      |
| Jin et al. [10]                                | Methods based on graphical representation; 2-3-4-5-6 dimensional graphical methods, Chaos game representation, quaternion. Matrix mapping, Coding based on chemical properties, Codons, frequency values, Position statistics, Huffman coding, Euclidean distance coding  | Detection of similarity between species        |
| Mendizabal-<br>Ruiz et al.<br>[11]             | Integer, Real, EIIP, Atomic number, Paired numeric, Voss, Tetrahedron, Z-curve, DNA walk  | Identification of similarity of DNA sequences  |
| Saini et al.<br>[12]                           | Voss, Tetrahedron, Complex, EIIp, DNA walk, Integer number, Real<br>number, Binary representation, 4-bit binary encoding, Paired nucleotide<br>representation, Quaternion, Inter-numcleotide distance   | Genomic signal processing                      |
| Mabrouk et al. [13]                            | Genetic code context, Frequency of nucleotide occurence, Atomic number, 2-bit binary, EIIP  | Identification of protein coding regions       |
| Das et al.<br>[14]                             | Voss mapping, Integer mapping, Complex Mapping, Real Mapping, EIIP<br>Mapping, Atomic Number Mapping, Paired Numeric Mapping, DNA<br>Walk Mapping, The Modecular Mass Mapping   | Identification of exon regions                 |
| Das et al.<br>[15]                             | Integer Mapping, Reel Mapping, Atomic Mapping, Molecular Mass Mass<br>Mapping, DNA Walk Mapping, Paired Numeric Mapping, Complex<br>Digital Mapping, EIIP   | Classification of exon and intron              |
| Abo-Zahhad<br>et al. [16]                      | Atomic number, Integer number, Real number, EIIP, Paired Numeric, DNA Walk  | Prediction of donor ve acceptor in exon region |
| Abo-Zahhad<br>et al. [17]                      | <ol> <li>Fixed Mapping</li> <li>Voss, Tetrahedron, Complex, Integer, Real, Quaternion</li> <li>Physico Chemical Property Based Mapping</li> <li>FIIP. Paired numeric. DNA-walk. Z-curve</li> </ol>  | Classification of exon and intron              |
| Kwan et al.<br>[18]                            | Integer number, Single Galois Indicator, Paired nucleotide atomic umber,<br>Atomic number, Molecular Mass, EIIP, Paired Numeric, Real Number,<br>Complex Number, K-twin pair code, K-bipolar pair code, K-quaternion  | Classification of exon and intron              |
| Sharma et al.<br>[19]<br>Akalin et al.<br>[20] | Voss, Tetrahedron, Z-curve, Complex, EIIP, Paired numeric, DNA walk,<br>Frequency Nucleotide Occurence, Atomic number, Real number<br>Real mapping, Moleculer Mass, EIIP, Shannon Entropy, Paired digital<br>mapping technique  | Identification of exon region                  |
| Akalin et al.<br>[21]                          | Real mapping, Moleculer Mass, EIIP, Shannon Entropy, Paired digital mapping technique   | Prediction of leukaemia                        |
| Akhtar et al.<br>[22]                          | Voss, Tetrahedron, Z-curve, Complex, Queternion, EIIP, QPSK-PAM, Paired numeric   | Prediction of exon regions                     |

In this study, all numerical mapping techniques developed in the last 15 years in the literature and used to digitize DNA sequences were examined and the benefits and shortcomings of these numerical techniques in genomic study areas such as exon region detection, exon-intron classification, phylogenetic analysis. Also, disease-causing gene detection were emphasized. Digitization of DNA sequences is extremely important in order to achieve targeted high-performance accuracy in genomic studies such as detection of exon regions, exon-intron classification, disease-causing gene detection, disease-causingene detection, disease-causing g

phylogenetic analysis. Therefore, in this study, all the digital mapping techniques of the last 15 years were introduced in detail and a review study presenting all the techniques was actualized.

# **1.2 Motivation**

Technological developments in biology and computers have advanced rapidly, and thus the emerging branch of bioinformatics has taken the lead among the most popular academic and industrial sectors today. Genome analysis is one of the most studied subjects in the field of bioinformatics, which is the synthesis of mathematics, statistics, computer science, molecular biology, and genetics. Although genomic studies seem to be aimed at basic scientific research, they will be indispensable for clinical informatics in the coming years. Our motivation for this review study is to analyze the effect of digital mapping techniques on the performance of the system in the most popular bioinformatics and genomic fields of study. In addition, while converting DNA analog signals into digital signals that can be understood by the computer in artificial intelligence applications, it is to guide researchers in choosing the correct digital coding technique that can best reflect the structure of DNA.

The remainder of this paper is organized as follows. In section 2, all numerical mapping techniques introduced in the literature by other authors in the last 5 years are searched and listed for this survey article. Section 3 highlights the frequency of use, performance, advantages, and drawbacks of numerical mapping techniques by genomic domains. In addition, mapping techniques that researchers can use according to genomic domains will be recommended along with their reasons. Finally, in Section 4 we conclude our survey with a brief summary.

# 2. DNA Numerical Mapping Techniques

In this section, the coding techniques developed for the digitization of DNA sequences are comprehensively examined under five main headings. In the literature, coding techniques are also called different names as digital mapping techniques, numerical methods, and coding schemes. However, all the nomenclatures mean the same. 50 digital mapping techniques developed in the last 5 years are classified into five groups according to their general characteristics. These groups are cartesian coordinate coding techniques, biochemical and physicochemical coding techniques, binary and information coding, primary structure coding techniques, and graphically represented coding techniques. At the end of each of these five groups, there are collective digital signal plot graphs and tables of the digital coding techniques examined in that group. Graphs of digitized DNA signals using coding techniques include representations of the DNA sequence digitized by each coding technique applied to the DNA Fasta format dataset with reference number NR 131216.1 from the NCBI database. Since the graphical value ranges of some mapping techniques are different, the numerical representation of these techniques is given in separate figures. In the general tables at the end of the examined groups, there is a brief explanation of the digitization technique in that group, the coding scheme, and the numerical version of this coding technique applied to a sample DNA sequence. Figure 2 shows the hierarchical scheme of all DNA mapping techniques.



Figure 2 The hierarchical scheme of all DNA mapping techniques

# 2.1 Cartesian-Coordinate Properties Group

The first group of DNA numerical mapping techniques is cartesian coordinate properties (CCP) digitization techniques. Within this group, there are nine numerical coding techniques namely Integer Number Coding, Real Number Coding, Complex Number Coding, DNA Walk Mapping, Trigonometric Mapping, Paired Numeric Coding, Ordinal Encoding, QPSK (Quadrature Phase Shift Keying), PAM (Pulse Amplitude Modulation) are examined. Table 2 provides a brief summary of all the mapping techniques in the CCP group.

|  | Table 2 The summary | v of all | numerical | coding | techniqu | ies in | cartesian | -coordinate | properties g | roup |
|--|---------------------|----------|-----------|--------|----------|--------|-----------|-------------|--------------|------|
|--|---------------------|----------|-----------|--------|----------|--------|-----------|-------------|--------------|------|

| The name of     | Coding Scheme      | Numerical Representation                           | Definition                   |
|-----------------|--------------------|--|------------------------------|
| technique       |                    |  |                              |
|                 | If Purin>Pirimidin | X = [AGCTACCGTG]                                   | Nucleotides are represented  |
| Integer Number  | T=0, C=1, A=2, G=3 | $\hat{\mathbf{v}}$ [2, 2, 1, 0, 2, 1, 1, 2, 0, 2]  | by integers.                 |
| Coding [6,15]   | T>A ve G>C ise     | X = [2, 3, 1, 0, 2, 1, 1, 3, 0, 3]                 |                              |
|                 | A=0, C=1, T=2, G=3 |  |                              |
|                 | A=-1.5, T=1.5,     | X=[AGCTACCGTG]                                     | Nucleotides are represented  |
| Real Number     | C=0.5, G=-0.5      | $\hat{X}$ =[-1.5, -0.5, 0.5, 1.5, -1.5, 0.5, 0.5,  | by real numbers.             |
| Coding [6,15]   |                    | -0.5, 1.5, -0.5]                                   |                              |
|                 |                    |  |                              |
|                 | A = -1, C = -j,    | X=[AGCTACCGTG]                                     | Nucleotides are represented  |
| Complex Number  | G= j, T= 1         | $\hat{X}(i) = [1, -1, j, j, 1, -j, -j, -1, j, -1]$ | by complex numbers.          |
| Coding [9]      |                    |  |                              |
|                 | Integer temsil;    | X=[AGCTACCGTG]                                     | Nucleotides are encoded by   |
| DNA Walk Coding | A = -1, C = 1      | $\hat{X}(i) = [-1, -2, -1, 0, -1, 0, 1, 0, 1, 0]$  | assigning integer or complex |
| [6]             | G=-1, T=1          |  | numbers and summing their    |
|                 | Complex temsil;    |  | C                            |

|   | A=1, C= -j<br>G= -1, T= j   |  | values along the DNA sequence.   |
|---|---|--|--|
| Trigonometric<br>Mapping Coding<br>[3,22] | $A = \cos(\theta) + j \times \sin(\theta)$ $C = -\cos(\theta) - j \times \sin(\theta)$ $G = -\cos(\theta) + j \times \sin(\theta)$ $T = \cos(\theta) - j \times \sin(\theta)$ | $\begin{split} &X{=}[AGCTACCGTG]\\ &\hat{X}(i) = [0.5{+}0.8660i, -0.5{+}0.8660i, \\ &-0.5{+}0.8660i, 0.5{+}0.8660i, 0.5{+}0.8660i, \\ &-0.5{+}0.8660i, -0.5{+}0.8660i \\ &-0.5{+}0.8660i, -0.5{+}0.8660i \\ &0.5{+}0.8660i, -0.5{+}0.8660i] \end{split}$ | Nucleotides are encoded by assigning trigonometric equations.  |
| Paired Numeric<br>Coding [15]             | Purin(A&G)= 1<br>Pirimidin(C&T)= -1   | X = [AGCTACCGTG]<br>$\hat{X} = [1, 1, -1, -1, 1, -1, -1, 1, -1, 1]$  | Nucleotides are encoded by assigning values according to their structural properties.                                |
| Ordinal Encoding<br>[23]                  | A= 0.25, C= 0.50<br>G= 0.75, T= 1.00  | $\begin{aligned} &X = [\text{AGCTACCGTG}] \\ &\hat{X}(i) = [0.25, 0.75, 0.50, 1.00, 0.25, 0.50, 0.50, 0.50, 0.75, 1.00, 0.50] \end{aligned}$   | Nucleotides are assigned sequential, linear values.  |
| QPSK [24]                                 | A= 1+j, G= -1+j<br>C= -1-j, T= 1-j  | X=[AGCTACCGTG]<br>$\hat{X}(i) = [1+j, -1+j, -1-j, 1-j, 1+j, -1-j, -1-j, -1+j, 1+j, -1+j]$  | 2D QPSK constellation<br>complex number values are<br>assigned according to the<br>complementary property of<br>DNA. |
| PAM [6,25]                                | A= -1.5, G= -0.5<br>C= 0.5, T= 0.5  | X=[AGCTACCGTG]<br>$\hat{X}(i) = [-1.5, -0.5, 0.5, 0.5, -1.5, 0.5, 0.5, -0.5, 0.5, -0.5]$   | Nucleotides are represented by 1D real numbers.  |

DNA sample datasets in Genbanks are available in Fasta format and are analog signals. Digitized signal representations of the first 100 bases of the sequence with reference number NR\_131216.1 retrieved from the NCBI database, with coding techniques in the "Cartesian-Coordinate Properties (CCP)" group are shown in Figure 3.



Figure 3 Numerical representations of CCP group techniques

# 2.2 Biochemical and Physicochemical Properties Group

The second group of DNA numerical mapping techniques is the biochemical and physicochemical (BPP) numerical techniques. Within this group, eleven coding schemes such as EIIP, Integrated EIIP, Atomic Number Coding, Paired Nucleotide Atomic Number Coding, Molecular Mass Representation, Entropic Segmentation Coding, Autoregressive Coding, Four Structural Features Coding, Thermodynamic Properties Coding, Genetic Code Context-Based Numerical coding, Walsh Code Based Numerical Mapping are examined. Table 3 provides a brief summary of all the mapping techniques in the BPP group.

| The name of                                  | The nome of Coding Scheme   |  |  |  |  |  |
|--|---|--|--|--|--|--|
| technique                                    | Coung Scheme  | Numerical Representation   | Definition   |  |  |  |
| EIIP coding [3,6,9]                          | C=0.1340, T=0.1335,<br>A=0.1260, G=0.0806   | X=[AGCTACCGTG]<br>$\hat{X}$ = [0.1260, 0.0806, 0.1340, 0.1335, 0.1260,<br>0.1340, 0.1340, 0.0806, 0.1335, 0.0806]  | Energy values are assigned to the nucleotides  |  |  |  |
| Integrated EIIP coding [26]                  | EIIP codes for 64 codons  | X=[AGCTACCGTG]<br>$\hat{X}$ = [0.3406, 0.3481, 0.3935, 0.3935, 0.3940,<br>0.3486, 0.3935, 0.2947]  | EIIP energy values are assigned to DNA codons.   |  |  |  |
| Atomic number coding [6]                     | C= 58, T= 66,<br>A= 70, G= 78   | X=[AGCTACCGTG]<br>$\hat{X}$ = [70, 78, 58, 66, 70, 58, 58, 78, 66, 78]   | Atomic numbers are assigned to nucleotides.  |  |  |  |
| Paired<br>nucleotide<br>atomic coding<br>[9] | A&G= 62, C&T= 42  | $\begin{aligned} X &= [\text{AGCTACCGTG}] \\ \hat{X}(i) &= [62, 62, 42, 42, 62, 42, 62, 42, 62] \end{aligned}$   | Atomic numbers are assigned to paired nucleotides.   |  |  |  |
| Molecular mass coding [9,15]                 | C= 110, G= 150,<br>A= 134, T= 125   | X=[AGCTACCGTG]<br>$\hat{X}(i) = [134, 150, 110, 125, 134, 110, 110, 150, 125, 150]$  | Molecular mass values are assigned to nucleotides.   |  |  |  |
| Entropic<br>segmentation<br>coding [9,27,28] | 12-Symbol alphabet<br>A <sub>1</sub> , A <sub>2</sub> , A <sub>3</sub> , C <sub>1</sub> , C <sub>2</sub> ,C <sub>3</sub> ,<br>G <sub>1</sub> , G <sub>2</sub> , G <sub>3</sub> , T <sub>1</sub> , T <sub>2</sub> , T <sub>3</sub><br>Calculates entropy by<br>array | $X = [AGTTAGTGCT]$ $\hat{X}(i) = [A_1 G_2 S_3 T_3 S_1 T_1 A_2 G_3 T_1 G_2 C_3]$  | DNA segments and stop<br>codons are represented by the<br>18-symbol alphabet.  |  |  |  |
| Autoregressive<br>coding [9,29]              | Propeller Twist ve<br>DNA Bending<br>Stiffness values for<br>dinükleotides  | $\begin{split} &X{=}[\text{AGCTACCGTG}]\\ &\text{Propeller Twist}\\ &\hat{X}(i) = [-14.00, -11.08, -14.00, -11.85, -13.10, -8.10, -10.03, -13.10, -9.45]\\ &\text{Bending Stiffness}\\ &\hat{X}(i) = [60, 85, 60, 20, 60, 130, 85, 60, 60] \end{split}$  | According to the structural<br>properties of DNA, propeller<br>twist and DNA bending<br>stiffness values and<br>dinucleotides are coded.   |  |  |  |
| Four Structural<br>features coding<br>[30]   | DNA Bending<br>Stiffness, Dublex<br>Disrupt Energy,<br>Dublex Free Energy,<br>Propeller Twist values<br>for dinükleotides   | $\begin{split} &X{=}[\text{AGCTACCGTG}] \\ &\text{DNA bending stiffness} \\ &\tilde{x}_{\alpha}(n) = 60, 60, 60, 85, 60 \\ &\text{Dublex disrupt energy} \\ &\tilde{x}_{\beta}(n) = 16, 16, 13, 36, 19 \\ &\text{Dublex free energy} \\ &\tilde{x}_{\gamma}(n) = {-}15, {-}15, {-}15, {-}28, {-}17 \\ &\text{Propeller twist} \\ &\tilde{x}_{\delta}(n) = {-}1400, {-}1400, {-}1310, {-}1003, {-}94 \end{split}$ | According to the four<br>physical properties of DNA,<br>the coding for the<br>dinucleotide is performed<br>according to the propeller<br>twist value, DNA bending<br>stiffness, duplex disrupts<br>energy, and duplex free<br>energy values. |  |  |  |
| Thermodynamic<br>properties coding<br>[6,31] | TC=5.6, GA=5.6,<br>CA=5.8, TG=5.8,<br>TA=6.0, AC=6.5,<br>GT=6.5, CT=7.8,<br>AG=7.8, AT=8.6,<br>TT=9.1, AA=9.1,  | <i>X</i> =[AGCTACCGTG]<br>$\hat{X}(i) = [7.8, 11.1, 7.8, 6.0, 6.5, 11.0, 11.9, 6.5, 5.8]$  | Coding is performed by<br>assigning enthalpy values of<br>thermodynamic interactions<br>of nucleotides.  |  |  |  |

| Table 3 The summary of all numerical | coding techniques | in biochemical | and physicochemical |
|--------------------------------------|-------------------|----------------|---------------------|
|                                      | properties group  |                |                     |

|   | CC=11.0,GG=11.0,<br>GC=11.1, CG=11.9  |   |  |
|---|---|---|--|
| Genetic code<br>context (GCC)<br>based numerical<br>coding [13] | Assignment of GCC-<br>based complex<br>number<br>representations to<br>amino acids (Table 8)                        | $X$ =[AGCTACCGTG]         Birinci çerçeve AGC TAC CGT         İkinci çerçeve GCT ACC GTG $\hat{X}(i) = [0.05 + 88.7i, 0.6 + 88.3i, 1.88 + 193i, 0.06 + 125.1i, 0.60 + 181.2i, 1.32 + 141.4i]$ | The DNA sequence is read<br>with a reading frame as<br>triplet codons. The sequence<br>is digitized by assigning<br>complex number values to<br>amino acids. |
| Walsh Code<br>Based coding<br>[5]                               | $\begin{array}{l} A=\!W_{A}\!=\!0000 \\ T=\!W_{T}\!=\!0011 \\ G=\!W_{G}\!=\!0101 \\ C=\!W_{C}\!=\!0110 \end{array}$ | $X = [AGCTACCGTG]$ $\hat{X}(i) = [00000101  011000110000$ 011001100101  00110101]   | The fourth-order Walsh codes are assigned to nucleotides   |

Digitized signal representations of the sample DNA sequence (NR\_131216.1) with EIIP and Integrated EIIP techniques are shown in Figure 4.



Figure 4 Numerical representations of EIIP and Integrated EIIP techniques

Digitized signal representations with the four structural features coding technique are shown in Figure 5.



Figure 5 Numerical representations of the four structural features coding

Figure 6 gives the digitized signal plot of the reference sequence NR\_131216.1 using the GCC-based coding technique.



Figure 6 Numerical representations of the GCC coding

Digitized signal representations of the first 100 bases of the NR\_131216.1 reference numbered sequences by coding techniques in the "Biochemical and Physicochemical Properties (BPP)" group are shown in Figure 7.



Figure 7 Numerical representations of BPP group techniques

# 2.3 Binary and Information Encoding Group

The third group of DNA numerical mapping techniques is cartesian coordinate (CCP) digitization techniques. Within this group, ten coding techniques as Voss Representation, One-Hot Coding, Pathogenicity Island Coding, Gradient Source Localization Coding, 2-bit Binary Encoding, Error Correction Code (ECC), I Ching Representation, Galois Field Representation, Gray Code Representation, K-mer Encoding are examined. Table 4 provides a brief summary of all the mapping techniques in the "Binary and Information Encoding" group.

| The name of<br>technique             | Coding Scheme  | Numerical Representation  | Definition   |
|--------------------------------------|--|---|--|
|                                      |  | X=[AGCTACCGTG]  |  |
|                                      | S = [C, G, A, T],  | $A_{20} = [1000100000]$   | By creating four sequences,  |
| Voss Coding                          | Gn=[0, 1, 0, 0],   | $G_{20} = [0100000101]$   | binary values are assigned   |
| [6]                                  | An=[0, 0, 1, 0],   | $C_{20} = [0010011000]$   | according to the presence or absence of each base.   |
|                                      | Tn=[0, 0, 0, 1]  | $T_{20} = [0001000010]$   |  |
|                                      | A:1.0.0.0  | X=[AGCTACCGTG]  | Nucleotides are encoded with   |
| One-hot<br>Coding [32]               | T:0,1,0,0<br>C:0,0,1,0<br>G:0,0,0,1  | $\hat{X}(i) = [1000, 0001, 0010, 0100, 1000, 0010, 0010, 0001, 0100, 0001]$   | four-bit binary values.  |
| Pathonetity                          |  | X=[AGCTACCGTG]  | Binary values are assigned   |
| Island Coding<br>[9,33]              | C&G= 1, A&T= 0   | $\hat{X}(i) = [0110011101]$   | according to the presence and absence of pathogenicity islands.  |
| Gradient                             |  | X=[AGCTACCGTG]  | Integer values are assigned to   |
| Source<br>Localization<br>Coding [9] | A= 0, C=1, G=3, T= 2   | $\hat{X}(i) = [0, 3, 1, 2, 0, 1, 1, 3, 2, 3]$   | nucleotides based on gradient source localization  |
|                                      |  | X=[AGCTACCGTG]  | Two-bit binary values are  |
| 2-bit Binary<br>Encoding [13]        | A= 00, G= 10,<br>T= 01, C= 11  | $\hat{X}(i) = [00, 10, 11, 01, 00, 11, 11, 10, 01, 10]$   | assigned to the nucleotides  |
|                                      |  | X=[AGCTACCGTG]  |  |
| Error<br>Correction<br>Coding [6,34] | x, y coordinates<br>values according to<br>group codons like<br>Purine-Pyrimidine,<br>Weak-Strong H bond,<br>Amino-Keto  | Purine-Prymidine<br>$\hat{X}(i) = [(1,1), (2,6), (3,5), (4,3), (5,6), (6,5), (7,3), (8,7)]$<br>Weak-Strong H bond<br>$\hat{X}(i) = [(1,1), (2,2), (3,4), (4,7), (5,1), (6,3), (7,2), (8,5)]$<br>Amino-Keto<br>$\hat{X}(i) = [(1,3), (2,7), (3,3), (4,6), (5,4), (6,5), (7,2), (8,0)]$ | Nükleotidlere biyokimyasal<br>özelliklerine göre x ve y<br>koordinat değerleri atanır                                    |
| IChing Coding<br>[6,35]              | Binary coding with 3<br>different I Ching<br>tables according to<br>amino acids  | X=[AGCTACCGTG]<br>$\hat{X}(i) = [110\ 100\ 001\ 010\ 100\ 001\ 010$<br>101]   | Coding is performed with I<br>Ching tables created according<br>to the three biochemical<br>properties of nucleic acids. |
| Galois Field<br>Coding [36]          | $\begin{array}{l} 0=0 \Leftrightarrow 0 \Leftrightarrow A, \\ x^{0}=1 \Leftrightarrow 1 \Leftrightarrow C, \\ x^{1}=x \Leftrightarrow 2 \Leftrightarrow T, \\ x^{2}=x+1 \Leftrightarrow 3 \Leftrightarrow G \end{array}$ | $X = [AGCTACCGTG]$ $\hat{X}(i) = [0, 3, 1, 2, 0, 1, 1, 3, 2, 3]$  | Nucleotides are assigned<br>numerical values corresponding<br>to their quadratic polynomial<br>representation.           |
| Gray Code<br>Coding [36]             | A= 00, T=01,<br>C=10, G= 11  | X = [AGCTACCGTG]<br>$\hat{X}(i) = [0010011100$<br>0101101110]   | Two-bit binary codes are<br>assigned to nucleotides by ex-or<br>operation.   |
| K-mer<br>Encoding<br>[37,38]         | 1-mer coding<br>A → [1,0,0,0]<br>C → [0,1,0,0]<br>G → [0,0,1,0]<br>T → [0,0,0,1]   | X=[AGCTACCGTG]<br>$\hat{X}(i) = [1000, 0010, 0100, 0001, 1000, 0100, 0010, 0001, 0010]$   | The DNA sequence is split into<br>k-mer degments and coded with<br>zeros and ones.                                       |

# Table 4 The summary of all numerical coding techniques in binary and information encoding group

Figure 7(a) gives the digitized signal plot of the sample sequence using the Voss coding technique and Figure 7(b) IChing coding technique.



Figure 8 gives the digitized signal representations of the first 100 bases of the NR\_131216.1 reference numbered sequences with the coding techniques in the "Binary and Information Encoding" group.



Figure 8 Numerical representations of BIE group techniques

# 2.4 Primary Structure Properties Group

Representation

[39,40]

placed on the unit circle

and coded according to

their positions.

The fourth group of DNA numerical mapping techniques are primary structure feature (PSP) digitization techniques. In this group, six coding techniques are examined, namely Dinucleotide Representation, Ring Structure Representation, Triplet Encoding, Frequency of Nucleotide Occurence Mapping, Entropy Based Numerical Mapping, Inter Nucletide Distance Representation. Table 5 provides a brief summary of all the mapping techniques in the "Primary Structure Properties" group.

| Tuble 5 The Summary of an numerical county techniques in Timary Structure Troperices group |                      |   |                               |  |  |  |
|--|----------------------|---|-------------------------------|--|--|--|
| The name of<br>technique   | Coding Scheme        | Numerical Representation                    | Definition                    |  |  |  |
|  |                      | X=[AGCTACCGTG]                              |                               |  |  |  |
| Dinucleotide   | 16 dinucleotides are | $\hat{X}(i) = [(\cos(\pi/2), \sin(\pi/2)),$ | Dinucleotides are distributed |  |  |  |

 $(\cos(13\pi/4), \sin(13\pi/4)),$ 

 $(\cos(15\pi/8), \sin(15\pi/8)),$ 

 $(\cos(3\pi/4), \sin(3\pi/4)),$  $(\cos(5\pi/8), \sin(5\pi/8)),$ 

Table 5 The summary of all numerical coding techniques in Primary Structure Properties group

evenly around a circle and coded

with their coordinate values.

|  |  | $(\cos(\pi/8), \sin(\pi/8)), (\cos(2\pi), Sin(2\pi)), (\cos(11\pi/8), Sin(11\pi/8)), (\cos(\pi), sin(\pi))]$      |   |
|--|--|---|---|
| Ring Structure<br>Representation<br>[6,41]             | AG: (0, 1.5), CT: (0, -<br>1.5), CA:(1,1), TG: (-1, -<br>1), CG: (1, -1), TA: (-1,<br>1), GA: (1, 0),GT(0.5, -<br>1.25), GC: (-0.5, 1.25),<br>TC: (-1, 0), AC: (-0.5,<br>1.25), AT: (0.5, 1.25),<br>AA: (0, 1), TT: (0.5, 0),<br>GG: (0,1), CC: (-0.5, 0). | X=[AGCTACCGTG]<br>$\hat{X}(i) = [(0, 1.5), (0, -1.5), (-0.5, 1.25), (1, -1), (-1, -1)]$                           | Dinucleotides are placed at the<br>corners of the hexagon according<br>to the six groups they are divided<br>into according to their<br>biochemical properties, and six<br>coding schemes are obtained with<br>six different combinations and<br>coded with the corner coordinates<br>of the hexagon. |
| Triplet Encoding<br>[6,42]                             | 64 codons are encoded by weights   | X=[AGCTACCGTG]<br>$\hat{X}(i) = [15.6, 1.1, 11.3, 18.2, 16.4, 14.4, 2.1, 19.4]$                                   | Nucleotide triplets and amino<br>acid codons are quantified by<br>weight.   |
| Frequency of<br>Occurence<br>Mapping [6,13]            | C=0.27215, T=0.2056,<br>A=0.24300, G=0.27909<br>or<br>CG:0.01, GC: 0.043, CC:<br>0.047, GT:0 .049, GG:<br>0.050, AC: 0.054, TC:<br>0.057, GA: 0.061,<br>TA:0.067, AG: 0.070,<br>CT: 0.071, TG: 0.074,<br>CA: 0.074, AT: 0.081,<br>AA: 0.097, TT: 0 .097    | X=[AGCTACCGTG]<br>$\hat{X}(i) = [0.070, 0.071, 0.054, 0.01, 0.074]$   | Nucleotides or dinucleotides are<br>coded with frequency values<br>according to their frequency of<br>occurrence.   |
| Entropy Based<br>Numerical<br>Mapping [43]             | Entropy values calculated<br>according to the new<br>formulas are assigned to<br>64 codons.  | X=[AGCTACCGTG]<br>$\hat{X}(i) = [0.7222, 0.8331, 0.9086, 0.8331, 0.8118, 0.5363, 0.6259, 0.9818, 0.9998, 0.9954]$ | The codons are coded by<br>calculating the entropy values of<br>the modified and fractional new<br>equation of Shannon's entropy<br>equation.   |
| Inter Nucleotide<br>Distance<br>Representation<br>[44] | Each base is encoded with<br>the value of the base<br>distance between the next<br>itself and the same base.   | X=[AGCTACCGTG]<br>$\hat{X}(i) = [4, 6, 3, 5, 5, 1, 3, 2, 1, 0]$   | Each base in the DNA sequence<br>is encoded with the base distance<br>value between it and the same<br>base that follows it.  |

Figure 9(a) gives the digitized signal plot of the reference sequence NR\_131216.1 using the Dinucleotide distance coding technique and Figure 9(b) The Ring Structure technique.



(a) Dinucleotide Distance (b) Ring Structure Figure 9 Numerical representations of Dinucleotide distance coding and the Ring Structure techniques

Figure 10 gives the digitized signal plot of the sample sequence using the Frequency of Nucleotide Occurrence coding technique.



Figure 10 Numerical representation of Frequency of Nucleotide Occurrence Coding

Figure 11 gives the digitized signal representations of the first 100 bases of the NR\_131216.1 reference numbered sequences with the coding techniques in the "Primary Structure Properties" group.

![](_page_12_Figure_5.jpeg)

Figure 11 Numerical representation of Primary Structure Properties Group

# 2.5 Graphical Representation Group

The fifth group of DNA numerical mapping techniques is Graphical Representation (GR) digitization techniques. Within this group, Tetrahedron Encoding, H-Curve Representation, Z-Curve Representation, Quaternion Encoding, SNP-GIN Encoding, Chaos Game Representation, (CGR), Chaos Game Representation Walk (CGR-Walk), Integer Chaos Game Representation (iCGR) Fourteen coding techniques are examined, namely, Som Based Approach, Fermat Spiral Curve Representation, Spectral Dynamic Representation, 2D Dynamic Representation, 3D Dynamic Representation, 8D Dynamic Representation. Table 6 provides a brief summary of all the mapping techniques in the "Graphical Representation" group.

| The name of technique                                       | Coding Scheme   | Numerical Representation  | Definition                            |
|---|---|---|---------------------------------------|
| <b>1</b>  |   | X=[AGCTACCGTG]  |                                       |
| Tetrahedron<br>Encoding<br>[6,45]                           | A=k,<br>G= $-\frac{2\sqrt{2}}{3}i - \frac{\sqrt{6}}{3}j - \frac{1}{3}k$ ,<br>C= $-\frac{2\sqrt{2}}{3}i + \frac{\sqrt{6}}{3}j - \frac{1}{3}k$ ,<br>T= $\frac{2\sqrt{2}}{3}i - \frac{1}{3}k$                                  | $\hat{X}_{1} = \begin{bmatrix} 0, -\frac{\sqrt{2}}{3}, -\frac{\sqrt{2}}{3}, \frac{2\sqrt{2}}{3}, 0, -\frac{\sqrt{2}}{3}, -\frac{\sqrt{2}}{3}, -\frac{\sqrt{2}}{3} \end{bmatrix}$  | Nucleotides are                       |
|   |   | $\frac{2\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}$  | corners of the                        |
|   |   |   | tetrahedron and coded by the          |
|   |   | $X_2 = \begin{bmatrix} 0, -\frac{1}{3}, \frac{1}{3}, 0, 0, \frac{1}{3}, \frac{1}{3}, -\frac{1}{3}, 0, \frac{1}{3} \end{bmatrix}$  | numerical<br>equations of the         |
|   |   | $\hat{X}_3 = \begin{bmatrix} 1, -\frac{1}{3}, -\frac{1}{3}, -\frac{1}{3}, 1, -\frac{1}{3}, -\frac{1}{3}, -\frac{1}{3}, -\frac{1}{3}, -\frac{1}{3}, -\frac{1}{3} \end{bmatrix}$  | corners.                              |
|   | $A = \frac{1}{2}i - \frac{\sqrt{3}}{2}j,$   |   | Nucleotides are                       |
| H-Curve   | $T = \frac{1}{2}i + \frac{\sqrt{3}}{2}j,$   | X=[AGCTACCGTG]  | encoded with<br>functions created     |
| Representation [6,46]                                       | $C = \frac{\sqrt{3}}{2}i + \frac{1}{2}j,$   | $\hat{X}_1 = [-0.3660i, 0.3660i, 1.3660i, 1.3660i, -0.3660i, 1.3660i, 1.3660i, 0.3660i, 1.3660i, 0.3660i]$  | by vectors i, and j                   |
|   | $G = \frac{\sqrt{3}}{2}i - \frac{1}{2}j$  |   | axes.                                 |
|   | $\hat{X}_{1}(i) \begin{cases} X(i-1) + 1 & if X(i) = \\ Y(i-1) + (-1) & other \end{cases}$  | X=[AGCTACCGTG]  | Nucleotides are                       |
| Z-Curve   | $\hat{X}_{2}(i) \{ X(i-1) + 1 \ if X(i) = $   | $\hat{X}_1 = [-1, 0, -1, 0, -1, -2, -3, -2, -1, 0]$   | encoded by sets of                    |
| Representation [6.47]                                       | (X(i-1) + (-1)) other<br>(X(i-1) + 1) if $X(i) = 1$   | $\hat{X}_2 = [1, 0, 1, 0, 1, 2, 3, 2, 1, 0]$  | vectors towards the four faces of     |
|   | $X_3(i)$ { $X(i-1) + (-1)$ other  | $A_3 = [1, 0, -1, 0, 1, 0, -1, -2, -1, -2]$   | the tetrahedron.                      |
|   |   | X=[AGCTACCGTG]  | Nucleotides are                       |
| Encoding  | A= $i+j+k$ , C=- $i+j-k$ , G=- $i-j+k$ ,<br>T- $i-i-k$  | $\hat{X}(i) = [i+j+k, -i-j+k, -i+j-k, i-j-k, i+j+k, -i+j-k, -i+j$ | represented by 4D                     |
| [6,18]  | 1–1 <sup>-</sup> J <sup>-</sup> K   | - <i>I</i> - <i>J</i> + <i>K</i> , <i>I</i> - <i>J</i> - <i>K</i> , - <i>I</i> - <i>J</i> + <i>K</i> ]  | equations.                            |
|   | $\begin{array}{l} 1000 \rightarrow A A \ veya \ A -\\ 0100 \rightarrow C C \ veya \ C -\\ 0010 \rightarrow G G \ veya \ G -\\ 0001 \rightarrow T T \ veya \ T -\\ 1100 \rightarrow A C, \ 1010 \rightarrow A G \end{array}$ | X=[AGCTACCGTG]  |                                       |
| SNP GIN   |   | $\hat{X}(i) =>$ Genotypes $\rightarrow A GC TA CC GT G$<br>Nucleotides $\rightarrow AGCTACCGTG$   | GINs are created<br>by assigning four |
| Encoding [49]   |   | Binary Encoding $\rightarrow$ 10100101110001100000  | pairs of SNPs to                      |
|   | $1001 \rightarrow A T, 0110 \rightarrow C G$<br>$0101 \rightarrow C T, 0011 \rightarrow G T$  | Hexadecimal $\rightarrow$ ASC60   | nucleondes.                           |
|   | A: (0, 0), T: (1, 0), G: (1, 1),<br>C: (0, 1)   | X=[AGCTACCGTG]  | The DNA sequence is                   |
| Chaos Game<br>Representation                                |   | $\hat{X}_1 = [(0,0), (0,0), (0.5, 0.5), (0.25, 0.75), (0.625, 0.75)]$   | mapped according                      |
| (CGR) [6,50]  |   | (0.375), (0.3125, 0.1875), (0.1563, 0.5938), (0.0781, 0.7969), (0.5391, 0.8984), (0.7695, 0.4492)]  | values within the                     |
|   |   | X=[AGCTACCGTG]  | unit square.                          |
|   | CGR <sub>RY</sub> : A(0, 0),T(1, 0),C(0,<br>1),G(1, 1)<br>CGR <sub>MK</sub> : A(0, 0),T(1, 0),G(0,<br>1),C(1, 1)<br>CGR <sub>WS</sub> : A(0, 0),G(1, 0),C(0,<br>1),T(1, 1)  | Purine-Prymidine  |                                       |
|   |   | $\hat{X}_1 = [[(0,0), (0,0), (0.5, 0.5), (0.25, 0.75), (0.625, 0.375),$   |                                       |
|   |   | (0.3125, 0.1875), (0.1563, 0.5938), (0.0781, 0.7969),   | The chaos game is                     |
| Chaos Game<br>Representation<br>Walk (CGR-<br>Walk) [51,52] |   | (0.5391, 0.8984), (0.7695, 0.4492)]]  | performed in the                      |
|   |   | Amino-Keto $\hat{\mathbf{x}}$ (0.0) (0.0) (0.05) (0.5 0.75) (0.75 0.275)  | walk, taking into                     |
|   |   | $X_1 = [(0,0), (0,0), (0, 0.5), (0.5, 0.75), (0.75, 0.575), (0.375, 0.1875), 0.6875, 0.5938), 0.8438, 0.7969)$  | account the thermodynamic             |
|   |   | (0.4219, 0.8984), 0.7109, 0.4492)]  | properties of                         |
|   |   | Weak-Strong   | DNA.                                  |
|   |   | $\hat{X}_1 = [(0,0), (0,0), (0.5, 0), (0.25, 0.5), (0.625, 0.75),$  |                                       |
|   |   | (0.3125, 0.375), (0.1563, 0.6875),(0.0781, 0.8438),   |                                       |
|   |   | (0.5391, 0.4219), (0.7695, 0.7109)]   |                                       |

# Table 6 The summary of all numerical coding techniques in Graphical representation group

| Integer Chaos<br>Game<br>Representation<br>(iCGR) [53] | A=(1,1), T=(-1,1), C=(-1,-1),<br>G=(1,-1)  | X=[AGCTACCGTG]<br>$\hat{X}_1 = [(1,1), (3, -1), (-1, -5), (-9,3), (7,19), (-25, -13), (-89, -77), (39, -205), (-217, 51), (295, -461)]$  | The Chaos game<br>representation is<br>performed with<br>integers rather<br>than floating-point<br>numbers.                                     |
|--|--|--|---|
| SOM Based<br>Approach<br>[6,54]                        | A: (0, 0, 0), T: (0.289, 0.5,<br>0.816),<br>C: (0.866, 0.5, 0), G: (0, 1, 0)   | $\begin{split} X &= [\text{AGCTACCGTG}] \\ \hat{X}_1 &= [(0,0,0), (0,1,0), (0.866, 0.5, 0), (0.289, 0.5, 0.816), \\ (0,0,0), (0.866, 0.5, 0), (0.866, 0.5, 0), (0,1,0), (0.289, 0.5, 0.816), (0,1,0)] \end{split}$ | Nucleotides are<br>paired with all<br>four corners.<br>Coding is<br>performed with<br>the distance values<br>between the AG<br>and CT vertices. |
| Fermat Spiral<br>Curve<br>Representation<br>[55]       | Representation of the four<br>sub-strings formed according<br>to the positions A, T, C, and<br>G in the Fermat spiral  | X=[AGCTACCGTG]<br>$\hat{X}_1 (Aseq)=[1,0,0,0,5,0,0,0,0,0]$<br>$\hat{X}_1 (Gseq)=[0,2,0,0,0,6,0,8,0,0]$<br>$\hat{X}_1 (Cseq)=[0,0,0,0,0,0,0,0,9,0]$<br>$\hat{X}_1 (Tseq)=[0,0,3,4,0,0,7,0,0,10]$                    | Global and local<br>location<br>information of<br>nucleotides in<br>DNA is mapped<br>on the Fermat<br>spiral.                                   |
| Spectral<br>Dynamic<br>Representation<br>[56]          | Representation of the<br>effusions of each base by a<br>series of lines  | $X=[AGCTACCGTG]$ $\hat{X}_1 (A)=[1,0,0,0,1,0,0,0,0,0]$ $\hat{X}_1 (G)=[0,1,0,0,0,1,0,1,0,0]$ $\hat{X}_1 (C)=[0,0,0,0,0,0,0,0,1,0]$ $\hat{X}_1 (T)=[0,0,1,1,0,0,1,0,0,1]$   | The distributions<br>of DNA<br>nucleotides are<br>represented by<br>four separate split<br>line plots.  |
| 2D Dynamic<br>Representation<br>[57]                   | A=(-1,0), G=(1, 0), C=(0, 1),<br>T=(0,-1)  | $X=[AGCTACCGTG]$ $\hat{X}_1 = [(-1,0), (0,0), (0,1), (0,0), (-1,0), (-1,1), (-1,2), (0,2), (0,1) (1,1)]$   | DNA sequences<br>are represented by<br>point masses in the<br>2D Euclidean<br>space.  |
| 3D Dynamic<br>Representation<br>[57,58]                | A=(-1, 0, 1), G=(1, 0, 1),<br>C=(0, 1, 1), T=(0, -1, 1)  | $X=[AGCTACCGTG]$ $\hat{X}_1 = [(-1,0,1), (0,0,2), (0,1,3), (0,0,4), (-1,0,5), (-1,1,6), (-1,2,7), (0,2,8), (0,1,9), (1,1,10)]$   | DNA/RNA<br>sequences are<br>represented in the<br>3D plane.   |
| 8D Vector<br>Representation<br>[59,60]                 | $A=(1, 0.2), T=(1, -0.2), C=(1, 0.3), G=(1, -0.3) z_i = y_i / i 	 K =(m_z, v_z) m_z = \frac{1}{n} \sum_{i=1}^n v_z = \frac{1}{n} \sum_{i=1}^n (z_i - m_z)^2$ | $X=[AGCTACCGTG]$ $\hat{X}_1 = [(1, 0.2), (2, -0.2), (3, 0.2), (4,0), (5, 0.2), (6, 0.5), (7, 0.8), (8, 0.5), (9, 0.3), (10, 0)]$ Slope=1.5370e-04 Variance=0.0182+0.0200i  | 8D vectors are<br>formed with mean,<br>variance values<br>from a zigzag plot<br>of DNA/RNA<br>sequences   |

Figure 12 (a) gives the digitized signal plot of the sample sequence using the tetrahedron encoding technique and (b) Z-Curve representation. Figure 13(a) gives the digitized signal plot of the sample sequence using the quaternion encoding Figure 13(b) Chaos Game representation. Figure 14 provides a digitized signal plot of the sample sequence according to the thermodynamic properties of purine-pyrimidine, amino-keto, and strong-weak H bonds using the Chaos game representation walk technique. Figure 15 gives the digitized signal plot of the sample sequence using the SOM-based coding technique.

![](_page_15_Figure_2.jpeg)

(a) Tedrahedron Encoding (b) Z-Curve Figure 12 Numerical representations of Tedrahedron Encoding and Z-Curve techniques

![](_page_15_Figure_4.jpeg)

(a) Quaternion (b) Chaos Game Figure 13 Numerical representations of Quaternion Encoding and Chaos Game techniques

![](_page_15_Figure_6.jpeg)

Figure 14 Numerical representation of Chaos Game Representation Walk (RY, MK, WS)

![](_page_16_Figure_1.jpeg)

Figure 15 Numerical representation of SOM based coding

Figure 16 gives the digitized signal plot of the sample sequence using the Fermat spiral curve coding technique.

![](_page_16_Figure_4.jpeg)

Figure 16 Numerical representation of Fermat spiral curve coding

Figure 17 gives a digitized signal plot of the sample sequence using the Spectral dynamic representation technique.

![](_page_16_Figure_7.jpeg)

Figure 17 Numerical representation of Spectral dynamic representation

Figure 18(a) gives the digitized signal plot of the sample array using the 2D dynamic representation technique, Figure 18(b) 3D dynamic, Figure 18(c) 8D dynamic.

# $\frac{1}{2}$ $\frac{1}$

# 3.Performance Comparison of Numerical Mapping Techniques in Genomic Fields

The aim of this review is to analyze how the digital mapping techniques (coding scheme -numerical methods), which are used for digitizing DNA sequences in bioinformatics studies and have gained popularity in recent years, affect performance in genomic fields. In this section, the frequency of use of DNA coding techniques for 4 popular genomic fields (identification of exon regions, exon-intron classification, phylogenetic analysis, gene detection) and the min-max range of the performances obtained using these techniques in that field was given. Figure 19 shows the most used numerical coding techniques for the identification of exon regions. Table 7 shows min-max performance intervals of the most used coding techniques for the identification of exon regions.

![](_page_17_Figure_4.jpeg)

Figure 19 The most used coding techniques for the identification of exon regions

| Coding<br>Technique                  | Min-Max<br>Performance<br>Interval (%) | Coding Technique         | Min-Max<br>Performance<br>Interval | Coding<br>Technique          | Min-Max<br>Performance<br>Interval |
|--------------------------------------|--|--------------------------|------------------------------------|------------------------------|------------------------------------|
| Integer                              | 36-81                                  | EIIP                     | 48-97                              | Voss                         | 60-92                              |
| Real                                 | 50-81                                  | IEEP                     | 80-88                              | One-hot                      | 70-90                              |
| Complex                              | 64-75                                  | Autoregressive           | 48-76                              | Binary                       | 65-75                              |
| DNA-Walk                             | 78-100                                 | Four structural features | 70-78                              | Pathogenity                  | 60-70                              |
| Trigonometric                        | 73-87                                  | Thermodynamic            | 70-80                              | Gray code                    | 65-80                              |
| Paired numeric                       | 47-94                                  | Genetic code context     | 66-79                              | K-mer                        | 85-93                              |
| Frequency<br>nucleotide<br>occurence | 81-100                                 | Walsh code               | 83-91                              | 8D vector                    | 70-75                              |
| Z-curve                              | 83-95                                  | Galois field             | 65-82                              | Atomic number                | 39-86                              |
| Inter nucleotide distance            | 80-85                                  | PAM                      | 58-75                              | Entropic segmentation        | 72-86                              |
| Tetrahedron                          | 71-79                                  | Entropy-based            | 92-100                             | Gradient Source localization | 65-80                              |
| Quaternion                           | 70-75                                  | Moleculer Mass           | 51-68                              | Paire dnucleotide atomic     | 80-86                              |

Table 7 Min-max performance intervals of the coding techniques in the identification of exon regions

As seen in Figure 19, the three most commonly used techniques for the identification of exon regions are EIIP, Paired numeric and Voss techniques, respectively. Looking at Table 7, it is seen that the performance values obtained in detecting exon regions with these three techniques are above 90%. However, although not used as often as these techniques in the literature, maximum 100% performance has been achieved in studies using Entropy-based, Frequency nucleotide occurrence, and DNA-Walk techniques. Therefore, this review is thought to increase the use of these techniques in the introduction of these techniques and in most genomic areas from now on. Figure 20 shows the most used numerical coding techniques for the classification of exon-intron.

![](_page_18_Figure_5.jpeg)

Figure 20 The most used coding techniques for the classification of exon-intron

Table 8 shows min-max performance intervals of the most used coding techniques for the classification of exon-intron.

| Coding<br>Technique    | Min-Max<br>Performance<br>Interval (%) | Coding Technique        | Min-Max<br>Performance<br>Interval | Coding<br>Technique      | Min-Max<br>Performance<br>Interval |
|------------------------|--|-------------------------|------------------------------------|--------------------------|------------------------------------|
| Complex                | 60-80                                  | DNA-Walk                | 67-95                              | Error correction code    | 60-70                              |
| Entropic segmentation  | 65-80                                  | Integer                 | 65-96                              | Entropy-based            | 92-96                              |
| 8D vector              | 70-80                                  | Real                    | 38-61                              | Galois field             | 70-75                              |
| Z-curve                | 80-86                                  | Binary                  | 70-88                              | Paired nucleotide atomic | 60-75                              |
| Voss                   | 75-88                                  | Paired-numeric          | 75-95                              | Moleculer mass           | 59-65                              |
| Tedrahedron            | 60-75                                  | Quaternion              | 66-95                              | IEIIP                    | 80-92                              |
| EIIP                   | 85-95                                  | Inter nucleotide atomic | 75-85                              | Atomic number            | 58-76                              |
| Four structure featues | 75-82                                  | One-hot                 | 64-80                              | H-curve                  | 60-76                              |

Table 8 Min-max performance intervals of the coding techniques in the classification of exon-intron

As seen in Figure 20, the three most commonly used techniques for the identification of exon regions are Complex, EIIP and Voss techniques, respectively. Looking at Table 8, while the performances of Complex and Voss techniques were above 80%, the performance increased up to 95% in studies conducted with the EIIP technique. Apart from these, Entropy-based, Integer, and EIIP techniques were used in studies with the highest performance in exon-intron classification. Figure 21 shows the most used numerical coding techniques for the phylogenetic analysis.

![](_page_19_Figure_6.jpeg)

Figure 21 The most used coding techniques for the phylogenetic analysis

Table 9 shows min-max performance intervals of the most used coding techniques for the phylogenetic analysis

| Coding<br>Technique | Min-Max<br>Performance<br>Interval (%) | Coding Technique          | Min-Max<br>Performance<br>Interval | Coding<br>Technique       | Min-Max<br>Performance<br>Interval |
|---------------------|--|---------------------------|------------------------------------|---------------------------|------------------------------------|
| CGR                 | 80-90                                  | Voss                      | 42-75                              | Quaternion                | 65-72                              |
| 2D                  | 78-90                                  | Tetrahedron               | 36-70                              | Entropy                   | 82-90                              |
| Fermat spiral       | 70-80                                  | Z-curve                   | 70-100                             | Four structural features  | 60-68                              |
| Integer             | 75-84                                  | H-curve                   | 70-80                              | CGR Walk                  | 50-60                              |
| Real                | 80-100                                 | DNA Walk                  | 75-88                              | Sprectral Dynamic         | 55-65                              |
| EIIP                | 86-98                                  | Dinucleotide              | 66-85                              | One-hot                   | 75-80                              |
| Atomic number       | 80-98                                  | Inter nucleotide distance | 75-80                              | Inter nucleotide distance | 55-72                              |
| Paired numeric      | 80-100                                 | 3D                        | 80-90                              | Triplet encoding          | 75-83                              |

Table 9 Min-max performance intervals of the coding techniques in the phylogenetic analysis.

As seen in Figure 21, the two most commonly used techniques for the phylogenetic analysis are CGR ve 2D techniques. Voss and Entropy-based techniques are the second most frequently used techniques after these. Looking at Table 9, Real and Z-Curve techniques were used in the highest performing studies for phylogenetic analysis. After these, EIIP and atomic number techniques were used in the studies with the highest performance. Figure 22 shows the most used numerical coding techniques for the detection of gene.

![](_page_20_Figure_5.jpeg)

Figure 22 The most used coding techniques for the detection of gene

Table 10 shows min-max performance intervals of the most used coding techniques for the detection of gene.

| Coding<br>Technique   | Min-Max<br>Performance<br>Interval (%) | Coding Technique     | Min-Max<br>Performance<br>Interval | Coding<br>Technique     | Min-Max<br>Performance<br>Interval |
|-----------------------|--|----------------------|------------------------------------|-------------------------|------------------------------------|
| CGR                   | 70-83                                  | Complex              | 65-75                              | One-hot                 | 78-96                              |
| Four structural       | 70-75                                  | Integer              | 63-99                              | Voss                    | 80-98                              |
| 2D                    | 70-75                                  | Real                 | 80-97                              | Pathogenity Island      | 65-75                              |
| Error correction code | 72-78                                  | Binary               | 91-100                             | EIIP                    | 61-100                             |
| H-curve               | 70-80                                  | Galois Field         | 70-75                              | Atomic number           | 65-97                              |
| Entropy               | 80-100                                 | Genetic code context | 62-79                              | Frequency of nucleotide | 72-100                             |

Table 10 Min-max performance intervals of the coding techniques in the detection of gene.

As seen in Figure 23, the three most commonly used techniques for gene detection are One-hot, EIIP, and Integer techniques, respectively. Looking at Table 10, success performances of 96%, 100%, and 99%, respectively, were obtained in gene screening studies using these techniques. Apart from these, 100% maximum success performance has been achieved in studies using the frequency of nucleotide technique and the Entropy-based technique, although it is not used very often.

# 4. Conclusion

This study is an attempt to review the DNA numerical mapping techniques used in the analysis of DNA sequences and to present the advantages and disadvantages of each technique to researchers. Each coding technique is exemplified in a DNA sequence, showing how that DNA sequence is digitized. Then, the frequency of use of these coding techniques in the 4 most popular study areas in the last 10 years and the max-min range of the performances obtained using these coding techniques were analyzed. This review will guide researchers in developing new coding techniques, and will facilitate previous researchers to improve their work. It will also guide researchers in discovering new techniques using innovative ideas.

# References

- R. H. Thomas. "Molecular Evolution and Phylogenetics. Masatoshi Nei and Sudhir Kumar. Oxford University Press, Oxford. 2000. pp. 333. Price £65.00, hardback. ISBN 0 19 513584 9.," *Heredity*, vol. 86, no. 3, pp. 385–385, 2001, doi: 10.1046/j.1365-2540.2001.0923a.x.
- [2] M. Akhtar, J. Epps, and E. Ambikairajah. "Signal Processing in Sequence Analysis: Advances in Eukaryotic Gene Prediction", *IEEE J. Sel. Top. Signal Process.*, vol. 2, no 3, pp 310-321, Jun. 2008, doi: 10.1109/JSTSP.2008.923854.
- [3] L. Das, J. K. Das, S. Mohapatra and S. Nanda. "DNA numerical encoding schemes for exon prediction: a recent history", *Nucleosides, Nucleotides & Nucleic Acids*, vol.40, no 10, pp. 985-1017, Oct. 2021, doi: 10.1080/15257770.2021.1966797.
- [4] U. N. Wisesty, T. R. Mengko and A. Purwarianti. "Gene mutation detection for breast cancer disease: A review", *IOP Conf. Ser.: Mater. Sci. Eng.*, vol. 830, no 3, pp. 032051, Apr. 2020, doi: 10.1088/1757-899X/830/3/032051.
- [5] M. Raman Kumar and N. K. Vaegae. "A new numerical approach for DNA representation using modified Gabor wavelet transform for the identification of protein coding regions", *Biocybernetics* and Biomedical Engineering, vol. 40, no 2, pp. 836-848, Apr. 2020, doi: 10.1016/j.bbe.2020.03.007.

- [6] N. Yu, Z. Li, and Z. Yu. "Survey on encoding schemes for genomic data representation and feature learning—from signal processing to machine learning", *Big Data Mining and Analytics*, vol. 1, no 3, pp. 191-210, Sep. 2018, doi: 10.26599/BDMA.2018.9020018.
- [7] P. K. Kumari, "A Survey on Numerical Representation of DNA Sequences", *Asian Journal For Convergence In Technology (AJCT) ISSN -2350-1146*, Apr. 2018.
- [8] L. Das, J. K. Das, S. Nanda and S. Mohapatra. "DNA Coding Sequence Prediction: A Review", içinde 2018 International Conference on Applied Electromagnetics, Signal Processing and Communication (AESPC), Oct. 2018, vol. 1, pp. 1-6. doi: 10.1109/AESPC44649.2018.9033278.
- [9] M. Ahmad, L. T. Jung and A.-A. Bhuiyan. "From DNA to protein: Why genetic code context of nucleotides for DNA signal processing? A review", *Biomedical Signal Processing and Control*, vol. 34, pp. 44-63, Apr. 2017, doi: 10.1016/j.bspc.2017.01.004.
- [10] X. Jin *et al.* "Similarity/dissimilarity calculation methods of DNA sequences: A survey", *Journal of Molecular Graphics and Modelling*, vol. 76, pp. 342-355, Sep. 2017, doi: 10.1016/j.jmgm.2017.07.019.
- [11] G. Mendizabal-Ruiz, I. Román-Godínez, S. Torres-Ramos, R. A. Salido-Ruiz and J. A. Morales, "On DNA numerical representations for genomic similarity computation", *PLOS ONE*, vol. 12, no 3, p. e0173288, Mar. 2017, doi: 10.1371/journal.pone.0173288.
- [12] S. Saini and L. Dewan. "Comparison of Numerical Representations of Genomic Sequences: Choosing the Best Mapping for Wavelet Analysis", *Int. J. Appl. Comput. Math*, vol. 3, no 4, pp. 2943-2958, Dec. 2017, doi: 10.1007/s40819-016-0277-1.
- [13] Mabrouk, M.S. Advanced Genomic Signal Processing Methods in DNA Mapping Schemes for Gene Prediction Using Digital Filters --Gene prediction, Digital filters, 3- Base periodicity, Exon, Intron, Bioinformatics, Genomic signal processing", *American Journal of Signal Processing*, p. 13, 2017.
- [14] L. Das, J. K. Das and S. Nanda, "Identification of exon location applying kaiser window and DFT techniques", içinde 2017 2nd International Conference for Convergence in Technology (I2CT), Apr. 2017, pp. 211-216. doi: 10.1109/I2CT.2017.8226123.
- [15] B. Das and I. Turkoglu. "Classification of DNA sequences using numerical mapping techniques and Fourier transformation, Journal of the Faculty of Engineering and Arcitecture of Gazi University, 2016, doi: 10.17341/gazimmfd.278447.
- [16] M. Abo-Zahhad, S. M. Ahmed and S. A. Abd-Elrahman. "Integrated Model of DNA Sequence Numerical Representation and Artificial Neural Network for Human Donor and Acceptor Sites Prediction", *IJITCS*, vol. 6, no 8, pp. 51-57, July. 2014, doi: 10.5815/ijitcs.2014.08.07.
- [17] M. Abo-Zahhad, S. M. Ahmed and S. A. Abd-Elrahman. "Genomic Analysis and Classification of Exon and Intron Sequences Using DNA Numerical Mapping Techniques", *IJITCS*, vol. 4, no 8, pp. 22-36, July. 2012, doi: 10.5815/ijitcs.2012.08.03.
- [18] H. K. Kwan, B. Y. M. Kwan and J. Y. Y. Kwan, "Novel methodologies for spectral classification of exon and intron sequences", *EURASIP Journal on Advances in Signal Processing*, vol. 2012, no 1, p. 50, Feb 2012, doi: 10.1186/1687-6180-2012-50.
- [19] S. D. Sharma, K. Shakya and S. N. Sharma, "Evaluation of DNA mapping schemes for exon detection", in 2011 International Conference on Computer, Communication and Electrical Technology (ICCCET), Mar. 2011, pp. 71-74. doi: 10.1109/ICCCET.2011.5762441.
- [20] F. Akalin and N. Yumusak. "Classification of exon and intron regions obtained using digital signal processing techniques on the DNA genome sequencing with EfficientNetB7 architecture", *GUMMFD*, 37:3 (2022) 1355-1371.
- [21] F. Akalin and N. Yumuşak. "Classification of ALL and CML malignancies being among the main types of leukaemia with graph neural networks and fuzzy logic algorithm," *GUMMFD*, Mar. 2022, doi: 10.17341/gazimmfd.1022624.
- [22] L. Das, S. Nanda and J. K. Das. "An integrated approach for identification of exon locations using recursive Gauss Newton tuned adaptive Kaiser window", *Genomics*, vol. 111, no 3, pp. 284-296, May. 2019, doi: 10.1016/j.ygeno.2018.10.008.
- [23] A. C. H. Choong and N. K. Lee. "Evaluation of convolutionary neural networks modeling of DNA sequences using ordinal versus one-hot encoding method", içinde 2017 International Conference

on Computer and Drone Applications (IConDA), Nov. 2017, pp. 60-65. doi: 10.1109/ICONDA.2017.8270400.

- [24] N. Chakravarthy, A. Spanias, L. D. Iasemidis and K. Tsakalis. "Autoregressive Modeling and Feature Analysis of DNA Sequences", *EURASIP J. Adv. Signal Process.*, vol. 2004, no 1, pp. 952689, Jan. 2004, doi: 10.1155/S111086570430925X.
- [25] R. M. Kumar and N. K. Vaegae. "Walsh code based numerical mapping method for the identification of protein coding regions in eukaryotes", *Biomedical Signal Processing and Control*, vol. 58, no. 101859, Ap. 2020, doi: 10.1016/j.bspc.2020.101859.
- [26] B. Das, S. Toraman, and I. Turkoğlu. "A novel genome analysis method with the entropy-based numerical technique using pretrained convolutional neural networks," *Turk J Elec Eng & Comp Sci*, vol. 28, no. 4, pp. 1932–1948, Jul. 2020, doi: 10.3906/elk-1909-119.
- [27] P. Bernaola-Galván, I. Grosse, P. Carpena, J. L. Oliver, R. Román-Roldán and H. E. Stanley. "Finding Borders between Coding and Noncoding DNA Regions by an Entropic Segmentation Method", *Phys. Rev. Lett.*, vol. 85, no 6, pp. 1342-1345, Aug. 2000, doi: 10.1103/PhysRevLett.85.1342.
- [28] D. Nicorici and J. Astola. "Segmentation of DNA into Coding and Noncoding Regions Based on Recursive Entropic Segmentation and Stop-Codon Statistics", *EURASIP J. Adv. Signal Process.*, vol. 2004, no 1, pp. 832471, Dec. 2004, doi: 10.1155/S1110865704309212.
- [29] N. Y. Song and H. Yan. "Autoregressive modeling of DNA features for short exon recognition", in 2010 IEEE International Conference on Bioinformatics and Biomedicine (BIBM), Dec. 2010, pp. 450-455. doi: 10.1109/BIBM.2010.5706608.
- [30] Q. Zheng, T. Chen, W. Zhou, L. Xie and H. Su. "Gene prediction by the noise-assisted MEMD and wavelet transform for identifying the protein coding regions", *Biocybernetics and Biomedical Engineering*, Vol. 41, no 1, 2021, doi: 10.1016/j.bbe.2020.12.005.
- [31] R. Harrison, Y. Li and I. Măndoiu, Ed. Bioinformatics Research and Applications: 11th International Symposium, ISBRA 2015 Norfolk, USA, June 7-10, 2015 Proceedings, c. 9096. Cham: Springer International Publishing, 2015. doi: 10.1007/978-3-319-19048-8.
- [32] Z. Abbas, H. Tayara and K. T. Chong. "4mCPred-CNN—Prediction of DNA N4-Methylcytosine in the Mouse Genome Using a Convolutional Neural Network", *Genes*, vol. 12, no 2, Feb. 2021, doi: 10.3390/genes12020296.
- [33] P. Liò and M. Vannucci. "Finding pathogenicity islands and gene transfer events in genome data", *Bioinformatics*, vol. 16, no 10, pp. 932-940, Oct. 2000, doi: 10.1093/bioinformatics/16.10.932.
- [34] L. Zhang, F. Tian, S. Wang and X. Liu. "A novel coding method for gene mutation correction during protein translation process", *Journal of Theoretical Biology*, vol. 296, pp. 33-40, Mar. 2012, doi: 10.1016/j.jtbi.2011.11.031.
- [35] F. Castro-Chavez. "Defragged Binary I Ching Genetic Code Chromosomes Compared to Nirenberg's and Transformed into Rotating 2D Circles and Squares and into a 3D 100% Symmetrical Tetrahedron Coupled to a Functional One to Discern Start from Non-Start Methionines through a Stella Octangula", *J Proteome Sci Comput Biol*, vol. 2012, no 1, pp. 3, 2012, doi: 10.7243/2050-2273-1-3.
- [36] M. Raman Kumar and V. Naveen Kumar. "A Numerical Representation Method for a DNA Sequence Using Gray Code Method", içinde Soft Computing for Problem Solving, Singapore, 2020, pp. 645-654. doi: 10.1007/978-981-15-0184-5\_55.
- [37] L. Deng, H. Wu, X. Liu and H. Liu. "DeepD2V: A Novel Deep Learning-Based Framework for Predicting Transcription Factor Binding Sites from Combined DNA Sequence", *International Journal of Molecular Sciences*, vol. 22, no 11, Jan. 2021, doi: 10.3390/ijms22115521.
- [38] Q. Zhang, Z. Shen and D.-S. Huang, "Modeling in-vivo protein-DNA binding by combining multiple-instance learning with a hybrid deep neural network", *Sci Rep*, vol. 9, no 1, p. 8484, June. 2019, doi: 10.1038/s41598-019-44966-x.
- [39] M. Randić, D. Butina and J. Zupan, "Novel 2-D graphical representation of proteins," *Chemical Physics Letters*, vol. 419, no. 4, pp. 528–532, Feb. 2006, doi: 10.1016/j.cplett.2005.11.091.
- [40] Z. Liu, B. Liao, W. Zhu and G. Huang, "A 2D graphical representation of DNA sequence based on dual nucleotides and its application", *International Journal of Quantum Chemistry*, vol. 109, no 5, pp. 948-958, 2009, doi: 10.1002/qua.21919.

- [41] A. T. M. Bari, M. Reaz, A. T. Islam, H.-J. Choi, and B.-S. Jeong. "Effective Encoding for DNA Sequence Visualization Based on Nucleotide's Ring Structure", *Evolutionary bioinformatics online*, vol. 9, pp. 251-61, July. 2013, doi: 10.4137/EBO.S12160.
- [42] S. Zou, L. Wang and J. Wang. "A 2D graphical representation of the sequences of DNA based on triplets and its application", *EURASIP Journal on Bioinformatics and Systems Biology*, vol. 2014, no 1, pp. 1, Jan 2014, doi: 10.1186/1687-4153-2014-1.
- [43] B. Das and I. Turkoglu. "A novel numerical mapping method based on entropy for digitizing DNA sequences", *Neural Comput & Applic*, vol. 29, 8: 207-215, Apr. 2018, doi: 10.1007/s00521-017-2871-5.
- [44] A. Sankar, A. Nair and M. Thiru. "Visualization of genomic data using inter-nucleotide distance signals", Jan. 2005.
- [45] Das, B. "A deep learning model for identification of diabetes type 2 based on nucleotide signals". Neural Comput & Applic (2022). https://doi.org/10.1007/s00521-022-07121-8
- [46] Das, B. "An implementation of a hybrid method based on machine learning to identify biomarkers in the Covid-19 diagnosis using DNA sequences", Chemometrics and Intelligent Laboratory Systems (2022), v. 230, 104680, ttps://doi.org/10.1016/j.chemolab.2022.104680
- [47] C.-T. Zhang and J. Wang. "Recognition of protein coding genes in the yeast genome at better than 95% accuracy based on the Z curve", *Nucleic Acids Research*, vol. 28, no 14, pp. 2804-2814, Tem. 2000, doi: 10.1093/nar/28.14.2804.
- [48] C. Yu, M. Deng, L. Zheng, R. L. He, J. Yang and S. S.-T. Yau, "DFA7, a New Method to Distinguish between Intron-Containing and Intronless Genes", *PLOS ONE*, vol. 9, no 7, pp. e101363, Tem. 2014, doi: 10.1371/journal.pone.0101363.
- [49] R. R. Garafutdinov, A. R. Sakhabutdinova, P. A. Slominsky, F. G. Aminev and A. V. Chemeris, "A new digital approach to SNP encoding for DNA identification", *Forensic Science International*, vol. 317, no. 110520, Dec. 2020, doi: 10.1016/j.forsciint.2020.110520.
- [50] T. Hoang, C. Yin and S. S.-T. Yau, "Numerical encoding of DNA sequences by chaos game representation with application in similarity comparison", *Genomics*, vol. 108, no 3, pp. 134-142, Oct 2016, doi: 10.1016/j.ygeno.2016.08.002.
- [51] W. Deng and Y. Luan, "Analysis of Similarity/Dissimilarity of DNA Sequences Based on Chaos Game Representation", *Abstract and Applied Analysis*, vol. 2013, p. e926519, Mar. 2013, doi: 10.1155/2013/926519.
- [52] Z.-G. Yu and V. Anh. "Time series model based on global structure of complete genome", *Chaos, Solitons & Fractals*, vol. 12, no 10, pp. 1827-1834, Aug. 2001, doi: 10.1016/S0960-0779(00)00147-8.
- [53] C. Yin, "Encoding and Decoding DNA Sequences by Integer Chaos Game Representation", *Journal of Computational Biology*, vol. 26, no 2, pp. 143-151, Feb. 2019, doi: 10.1089/cmb.2018.0173.
- [54] A. P. Boyle *et al.*, "Comparative analysis of regulatory information and circuits across distant species", *Nature*, vol. 512, no 7515, Aug. 2014, doi: 10.1038/nature13668.
- [55] Z. Mo et al., "One novel representation of DNA sequence based on the global and local position information", *Sci Rep*, vol. 8, no 1, p. 7592, May. 2018, doi: 10.1038/s41598-018-26005-3.
- [56] D. Bielińska-Wąż and P. Wąż, "Spectral-dynamic representation of DNA sequences", *Journal of Biomedical Informatics*, vol. 72, pp. 1-7, Aug. 2017, doi: 10.1016/j.jbi.2017.06.001.
- [57] A. Czerniecka, D. Bielińska-Wąż, P. Wąż, and T. Clark, "20D-dynamic representation of protein sequences", *Genomics*, vol. 107, no 1, pp. 16-23, Jan. 2016, doi: 10.1016/j.ygeno.2015.12.003.
- [58] D. Zhang. "A New Numerical Method for DNA Sequence Analysis Based on 8-Dimensional Vector Representation", *Journal of Applied Mathematics and Physics*, vol. 7, no 12, Dec. 2019, doi: 10.4236/jamp.2019.712204.
- [59] F. Ben Nasr, and A. E. Oueslati, "CNN for human exons and introns classification", içinde 2021 18th International Multi-Conference on Systems, Signals Devices (SSD), Mar. 2021, pp. 249-254. doi: 10.1109/SSD52085.2021.9429303.
- [60] A. Rokas, "Phylogenetic Analysis of Protein Sequence Data Using the Randomized Axelerated Maximum Likelihood (RAXML) Program", *Current Protocols in Molecular Biology*, vol. 96, no 1, pp. 19.11.1-19.11.14, 2011, doi: 10.1002/0471142727.mb1911s96.